

$$v_o = 1000 \frac{\text{m}}{\text{s}} \quad x = 2000\text{m} \quad y = 800\text{m}$$

What is θ_o ?

Method I

Using

$$y = x \tan \theta_o + \frac{g}{2 \cdot v_o^2 \cdot \cos^2 \theta_o} x^2$$

$$800 = 2000 \tan \theta_o - \frac{19.6}{\cos^2 \theta_o}$$

$$800 = 2000 \frac{\sin(\theta_o)}{\cos(\theta_o)} - \frac{19.6}{(\cos(\theta_o))^2}$$

$$A := \begin{pmatrix} -2.7512469174935126092 \\ -1.5806356857788123621 \\ 1.5609569678109808763 \\ .39034573609628062922 \end{pmatrix} \quad \left(\frac{180}{\pi} \right) \cdot A = \begin{pmatrix} -157.635 \\ -90.564 \\ 89.436 \\ 22.365 \end{pmatrix}$$

Note: A numerical solution (as mentioned in class) works nicely. Note that we would get rid of the 1st 2 solutions as they are negative values and would indicate an angle below the horizontal (which makes no sense). Thus the answers are 89.4° and 22.4° .

Method II

$$800(\cos(\theta_o))^2 = 2000 \cos(\theta_o) \cdot \sin(\theta_o) - 19.6$$

$$\text{Using} \quad \sin \theta_o = \sqrt{1 - (\cos(\theta_o))^2}$$

$$800(\cos(\theta_o))^2 = 2000 \cos(\theta_o) \cdot \sqrt{1 - (\cos(\theta_o))^2} - 19.6$$

Simplifying

$$\cos(\theta_0)^4 - .85531(\cos(\theta_0))^2 + .0000827586 = 0$$

Using the Quadratic Equation:

$$(\cos(\theta_0))^2 = \frac{.85531 + \sqrt{(.85531)^2 - 4 \cdot 1 \cdot (.0000827586)}}{2} = .85521323044937399500$$

$$\cos(\theta_0) = \sqrt{.85521323044937399500} = .925$$

$$\theta_0 = 22.4^\circ$$

$$(\cos(\theta_0))^2 = \frac{.85531 - \sqrt{(.85531)^2 - 4 \cdot 1 \cdot (.0000827586)}}{2} = 9.67695506260050250000^{-5}$$

$$\cos(\theta_0) = \sqrt{9.67695506260050250000^{-5}} = .009837$$

$$\theta_0 = 89.4^\circ$$

Note again here we have left out the negative roots as they do not provide meaningful information. The answers again are as previously calculated, except without numerical integration.