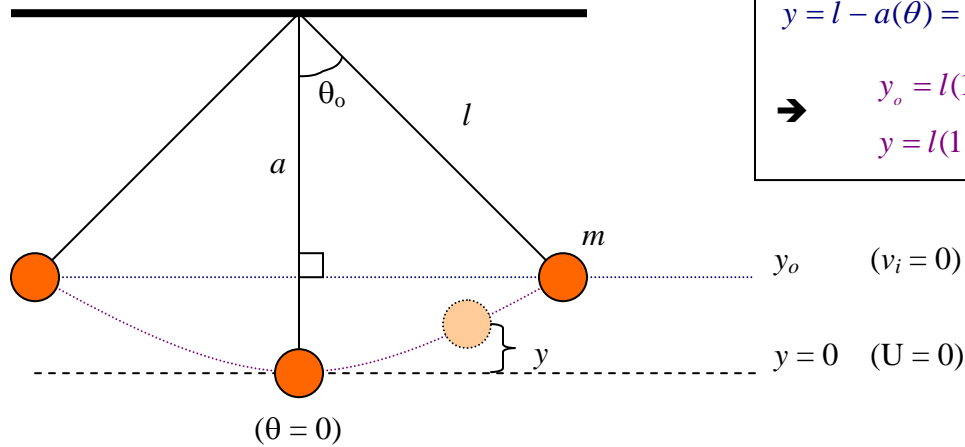


# Swinging Pendulum



$$a(\theta) = l \cos \theta$$

$$y = l - a(\theta) = l - l \cos \theta = l(1 - \cos \theta)$$

$$\rightarrow \begin{aligned} y_0 &= l(1 - \cos \theta_0) \\ y &= l(1 - \cos \theta) \end{aligned}$$

a) What is the tangential speed of mass  $m$  as a function of  $y$ ?

$$E_i = E_f$$

$$\frac{1}{2} m v_i^2 + m g y_0 = \frac{1}{2} m v^2 + m g y$$

$$0 + m g y_0 = \frac{1}{2} m v^2 + m g y$$

$$v = \sqrt{2g(y_0 - y)}$$

b) What is the tangential speed of mass  $m$  as a function of  $\theta$ ?

$$v = \sqrt{2g([l(1 - \cos \theta_0)] - [l(1 - \cos \theta)])}$$

$$v = \sqrt{2gl(1 - \cos \theta_0 - 1 + \cos \theta)}$$

$$v = \sqrt{2gl(\cos \theta - \cos \theta_0)}$$

c) What is the tangential speed of mass  $m$  at  $\theta = 0$ ?

$$v = \sqrt{2gl(1 - \cos \theta_0)}$$